

# The Moral Principle of Action–Motivation

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## 1 Introduction of the Principle

Immanuel Kant’s Categorical Imperative is to act according to that maxim which you can simultaneously will to be a universal law. However, I think that there are no maxims regarding actions alone that may be coherently willed universally, because one can easily contrive a situation where any action is permissible to prevent a greater evil. Instead, there are combinations of actions and sets of motivations that may coherently be willed to be prohibited or permissible. I propose the following augmentation of Kant’s formalization:

**Act according to the tuple of action and motivation set which you can simultaneously will to be universally permissible.**

## 2 Explication of Terms

Let us formalize the terms used in this principle. We consider an agent deliberating over actions.

- Let  $A$  be the set of possible actions available to the agent.
- Let  $B$  be the set of equivalence classes of statements of beliefs of the agent (modulo synonymous phrasing). We denote statements using double quotation marks, e.g., “This is a statement.”
- Let  $C$  be the set of *relevant anticipated states of affairs*, i.e. anticipated states of affairs that the agent believes to be made more likely by one possible action than by another, i.e.

$$c \in C \iff \exists a, a' \in A, \exists b \in B : \text{“}P(c|a) > P(c|a')\text{”} \in b.$$

Note that we assume that the agent considers a prior probability distribution over anticipated states of affairs that may be conditioned on actions, and note that the statement, “ $P(c|a) > P(c|a')$ ,” reflects the agent’s belief. This set therefore captures the states of affairs that are at issue to the agent in the present decision.

- Let  $d : A \rightarrow \{0, 1\}$  be a one-hot indicator function that signals the action decided upon by the agent, i.e.  $d(a) = 1$  if the agent decides to take action  $a$ , and  $d(a) = 0$  otherwise.
- Let  $e : A \rightarrow \mathcal{P}(C)$ , where  $\mathcal{P}$  denotes the power set, associate an action  $a$  with the subset of anticipated states of affairs that are relevant with respect to  $a$ , i.e.

$$e(a) = \{c \in C \mid \exists b \in B, \exists a' \in A : "P(c|a) \neq P(c|a')" \in b\}.$$

- Let the *motivation set*  $M_a$  of an action  $a$  be defined as the family of minimal subsets of  $e(a)$  that, if the agent believed them irrelevant, then action  $a$  would surely not be chosen, i.e.:

$$M_a = \{m \subseteq e(a) \mid \exists b \in B : "e(a) \cap m = \emptyset" \in b \implies d(a) = 0 \text{ and } \emptyset \neq m' \subset m \implies m' \notin M_a\}$$

The first condition above,  $\exists b \in B : "e(a) \cap m = \emptyset" \in b \implies d(a) = 0$ , means that a set  $m$  of states of affairs is in the motivation set of the agent with respect to action  $a$  if it is the case that if the agent were to believe (mistakenly or hypothetically) that the anticipated states of affairs represented by  $m$  were all not relevant with respect to  $a$ , then the agent would surely not take action  $a$ . The second condition,  $\emptyset \neq m' \subset m \implies m' \notin M_a$ , stipulates that no nonempty proper subset of such a set  $m$  is also contained in the motivation set. This enforces minimality of the included sets.

**Illustration (conjunctive):** Suppose Carl is choosing between staying at their current job or leaving it to find another. Then  $A = \{\text{stay}, \text{change}\}$ . Suppose that changing jobs offers a better salary and a shorter commute but requires more hours. Suppose further that if, hypothetically, a better salary and a shorter commute were *both* irrelevant to the decision (because, for example, neither action would change either of these figures), then Carl would surely not change jobs; but if either remains relevant, then he would be willing to change jobs. Then:

$$\{\{\text{better salary}, \text{shorter commute}\}\} \subseteq M_{\text{change}}$$

**Illustration (disjunctive):** Now suppose that if *either* a better salary or a shorter commute were not relevant (because, for example, neither action would change the figure), then Carl would surely not change jobs. Then:

$$\{\{\text{better salary}\}, \{\text{shorter commute}\}\} \subseteq M_{\text{change}}$$

Note that without the second condition specified above (enforcing minimality of elements of  $M_a$ ), we would also have  $\{\text{better salary}, \text{shorter commute}\} \in M_{\text{change}}$ . The condition avoids the

redundancy of such supersets, which is in general combinatorially explosive.

- For a given decision-making event, and for the action  $a$  for which  $d(a) = 1$ , the corresponding  $(a, M_a)$  represents the tuple of action and motivation set, as mentioned in the Rule.

### 3 Advantages of this Formulation

This Rule allows one to judge the morality of an action *both* by the nature of the action itself *and* by what consequences the decision-making agent believes it is making more or less likely by taking the action. In particular, it stipulates that the tuple of action and motivation set must be universally permissible.

### 4 Examples of Universalizable Maxims

- Do not lie for the purpose of attaining material personal benefit.
- Do not commit violence for the purpose of attaining material personal benefit.
- Seek out perspectives different from your own for the purpose of better understanding the consequences of your decisions.